Package ‘HiLDA’

March 13, 2024

**Type** Package

**Title** Conducting statistical inference on comparing the mutational exposures of mutational signatures by using hierarchical latent Dirichlet allocation

**Depends** R(>= 4.1), ggplot2

**Imports** R2jags, abind, cowplot, grid, forcats, stringr, GenomicRanges, S4Vectors, XVector, Biostats, GenomicFeatures, BSgenome.Hsapiens.UCSC.hg19, BiocGenerics, tidyr, grDevices, stats, TxDb.Hsapiens.UCSC.hg19.knownGene, utils, methods, Rcpp

**Suggests** knitr, rmarkdown, testthat, BiocStyle

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**Description** A package built under the Bayesian framework of applying hierarchical latent Dirichlet allocation. It statistically tests whether the mutational exposures of mutational signatures (Shiraishi-model signatures) are different between two groups. The package also provides inference and visualization.

**License** GPL-3

**URL** [https://github.com/USCbiostats/HiLDA](https://github.com/USCbiostats/HiLDA), [https://doi.org/10.1101/577452](https://doi.org/10.1101/577452)

**BugReports** [https://github.com/USCbiostats/HiLDA/issues](https://github.com/USCbiostats/HiLDA/issues)

**SystemRequirements** JAGS 4.0.0

**biocViews** Software, SomaticMutation, Sequencing, StatisticalMethod, Bayesian

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**VignetteBuilder** knitr

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boundaryTurbo_F

Check whether the parameter F is within the appropriate range

Description
Check whether the parameter F is within the appropriate range

Usage
boundaryTurbo_F(turboF, fdim, signatureNum)

Arguments
- turboF: F (converted for turboEM)
- fdim: a vector specifying the number of possible values for each mutation signature
- signatureNum: the number of mutation signatures

Value
a logical value

boundaryTurbo_Q

Check whether the parameter Q is within the appropriate range

Description
Check whether the parameter Q is within the appropriate range

Usage
boundaryTurbo_Q(turboQ, signatureNum, sampleNum)

Arguments
- turboQ: Q (converted for turboEM)
- signatureNum: the number of mutation signatures
- sampleNum: the number of cancer genomes

Value
a logical value
**convertFromTurbo_F**

*Description*

Restore the converted parameter F for turboEM

*Usage*

```r
convertFromTurbo_F(turboF, fdim, signatureNum, isBackground)
```

*Arguments*

- `turboF`: F (converted for turboEM)
- `fdim`: a vector specifying the number of possible values for each mutation signature
- `signatureNum`: the number of mutation signatures
- `isBackground`: the logical value showing whether a background mutation features is included or not

*Value*

a vector

---

**calcPMSLikelihood**

*A function for calculating the log-likelihood from the data and parameters*

*Description*

A function for calculating the log-likelihood from the data and parameters

*Usage*

```r
calcPMSLikelihood(p, y)
```

*Arguments*

- `p`: this variable includes the parameters for mutation signatures and membership parameters
- `y`: this variable includes the information on the mutation features, the number of mutation signatures specified and so on

*Value*

a value
**convertFromTurbo_Q**

*Restore the converted parameter Q for turboEM*

**Description**

Restore the converted parameter Q for turboEM

**Usage**

```r
canvertFromTurbo_Q(turboQ, signatureNum, sampleNum)
```

**Arguments**

- `turboQ`: Q (converted for turboEM)
- `signatureNum`: the number of mutation signatures
- `sampleNum`: the number of cancer genomes

**Value**

a vector

---

**convertToTurbo_F**

*Convert the parameter F so that turboEM can treat*

**Description**

Convert the parameter F so that turboEM can treat

**Usage**

```r
canvertToTurbo_F(vF, fdim, signatureNum, isBackground)
```

**Arguments**

- `vF`: F (converted to a vector)
- `fdim`: a vector specifying the number of possible values for each mutation signature
- `signatureNum`: the number of mutation signatures
- `isBackground`: the logical value showing whether a background mutation features is included or not

**Value**

a vector
**convertToTurbo_Q**  
*Convert the parameter Q so that turboEM can treat*

**Description**  
Convert the parameter Q so that turboEM can treat

**Usage**  
`convertToTurbo_Q(vQ, signatureNum, sampleNum)`

**Arguments**
- *vQ*  
  Q (converted to a vector)
- *signatureNum*  
  the number of mutation signatures
- *sampleNum*  
  the number of cancer genomes

**Value**  
a vector

---

**EstimatedParameters-class**  
*An S4 class representing the estimated parameters*

**Description**  
An S4 class representing the estimated parameters

**Slots**
- *sampleList*  
a list of sample names observed in the input mutation data
- *signatureNum*  
the number of mutation signatures specified at the time of estimation
- *isBackground*  
the flag showing whether the background signature data is used or not.
- *backGroundProb*  
the background signatures
- *signatureFeatureDistribution*  
estimated parameters for mutation signatures
- *sampleSignatureDistribution*  
estimated parameters for memberships of mutation signatures for each sample
- *loglikelihood*  
the log-likelihood value for the estimated parameters
**getLogLikelihoodC**

*Calculate the value of the log-likelihood for given parameters*

**Description**

Calculate the value of the log-likelihood for given parameters

**Usage**

```r
getLogLikelihoodC(
  vPatternList, 
  vSparseCount, 
  vF, 
  vQ, 
  fdim, 
  signatureNum, 
  sampleNum, 
  patternNum, 
  samplePatternNum, 
  isBackground, 
  vF0
)
```

**Arguments**

- `vPatternList`: The list of possible mutation features (converted to a vector)
- `vSparseCount`: The table showing (mutation feature, sample, the number of mutation) (converted to a vector)
- `vF`: F (converted to a vector)
- `vQ`: Q (converted to a vector)
- `fdim`: a vector specifying the number of possible values for each mutation signature
- `signatureNum`: the number of mutation signatures
- `sampleNum`: the number of cancer genomes
- `patternNum`: the number of possible combinations of all the mutation features
- `samplePatternNum`: the number of possible combination of samples and mutation patterns
- `isBackground`: the logical value showing whether a background mutation features is included or not
- `vF0`: a background mutation features

**Value**

a value
getMutationFeatureVector

*Get mutation feature vector from context sequence data and reference and alternate allele information*

**Description**

Get mutation feature vector from context sequence data and reference and alternate allele information

**Usage**

```r
getMutationFeatureVector(
  context, ref_base, alt_base,
  strandInfo = NULL, numBases, type
)
```

**Arguments**

- `context`: the context sequence data around the mutated position. This should be Biostrings::DNAStringSet class
- `ref_base`: the reference bases at the mutated position.
- `alt_base`: the alternate bases at the mutated position.
- `strandInfo`: transcribed strand information at the mutated position. (this is optional)
- `numBases`: the number of flanking bases around the mutated position.
- `type`: the type of mutation feature vector (should be "independent" or "full").

**Value**

a mutation feature vector

---

**hildaBarplot**

*Read the raw mutation data with the mutation feature vector format, estimate and plot both mutation signatures and their fractions*

**Description**

Read the raw mutation data with the mutation feature vector format, estimate and plot both mutation signatures and their fractions
hildaDiffPlot

Usage

hildaBarplot(
  inputG,
  hildaResult,
  sigOrder = NULL,
  refGroup,
  sortSampleNum = TRUE,
  refName = "Control",
  altName = "Case",
  charSize = 3
)

Arguments

inputG a MutationFeatureData S4 class output by the pmsignature.

hildaResult a rjags class output by HiLDA.

sigOrder the order of signatures if needed (default: NULL).

refGroup the samples in the reference group (default: NULL).

sortSampleNum whether to sort plots by number of mutations (default: TRUE).

refName the name of reference group (default: Control)

altName the name of the other group (default: Case)

charSize the size of the character on the signature plot (default: 3)

Value

a list of a signature plot and a barplot of mutational exposures

Examples

load(system.file("extdata/sample.rdata", package="HiLDA"))
inputFile <- system.file("extdata/hildaLocal.rdata", package="HiLDA")
hildaLocal <- readRDS(inputFile)

hildaBarplot(G, hildaLocal, refGroup=1:4)

hildaDiffPlot

Read the raw mutation data with the mutation feature vector format,
estimate and plot both mutation signatures and their fractions

Description

Read the raw mutation data with the mutation feature vector format, estimate and plot both mutation signatures and their fractions
Usage

hildaDiffPlot(inputG, hildaResult, sigOrder = NULL, charSize = 3)

Arguments

inputG a MutationFeatureData S4 class output by the pmsignature.
hildaResult a rjags class output by HiLDA.
sigOrder the order of signatures if needed (default: NULL).
charSize the size of the character on the signature plot (default: 3)

Value

a list of the signature plot and the mean difference plot.

Examples

load(system.file("extdata/sample.rdata", package="HiLDA"))
inputFile <- system.file("extdata/hildaLocal.rdata", package="HiLDA")
hildaLocal <- readRDS(inputFile)

hildaDiffPlot(G, hildaLocal)

---

hildaGlobalResult Compute the Bayes factor

Description

Compute the Bayes factor

Usage

hildaGlobalResult(jagsOutput, pM1 = 0.5)

Arguments

jagsOutput the output jags file generated by the jags function from the R2jags package.
pM1 the probability of sampling the null (default: 0.5)

Value

a number for the Bayes factor
Examples

```r
load(system.file("extdata/sample.rdata", package="HiLDA"))
hildaGlobal <- hildaTest(inputG=G, numSig=3, refGroup=1:4, nIter=1000, localTest=TRUE)
hildaGlobalResult(hildaGlobal)
```

---

**hildaLocalResult**

*Extract the posterior distributions of the mean differences in mutational exposures*

Description

Extract the posterior distributions of the mean differences in mutational exposures

Usage

```r
hildaLocalResult(jagsOutput)
```

Arguments

- `jagsOutput`: the output jags file generated by the jags function from the R2jags package.

Value

A data frame that contains the posterior distributions of difference.

Examples

```r
inputFile <- system.file("extdata/hildaLocal.rdata", package="HiLDA")
hildaLocal <- readRDS(inputFile)
hildaLocalResult(hildaLocal)
```

---

**hildaPlotSignature**

*Plot mutation signatures from HiLDA output*

Description

Plot mutation signatures from HiLDA output

Usage

```r
hildaPlotSignature(hildaResult, sigOrder = NULL, colorList = NULL, ...)
```
hildaReadMPFile

Arguments

- `hildaResult`: a `rjags` class output by HiLDA
- `sigOrder`: the order of signatures if needed (default: `NULL`)
- `colorList`: a vector of color for mutational exposures barplots
- `...`: additional arguments passed on to `visPMS`

Value

A plot object containing all mutational signatures

Examples

```r
inputFile <- system.file("extdata/hildaLocal.rdata", package="HiLDA")
hildaLocal <- readRDS(inputFile)
hildaPlotSignature(hildaLocal)
```

Description

The mutation position format is tab-delimited text file, where the 1st-5th columns shows sample names, chromosome names, coordinates, reference bases (A, C, G, or T) and the alternate bases (A, C, G, or T), respectively. An example is as follows:

```
  sample1 chr1 100 A C
  sample1 chr1 200 A T
  sample1 chr2 100 G T
  sample2 chr1 300 T C
  sample3 chr3 400 T C
```

Also, this function usually can accept compressed files (e.g., by gzip, bzip2 and so on) when using recent version of R.

Usage

```r
hildaReadMPFile(
  infile,
  numBases = 3,
  trDir = FALSE,
  bs_genome = NULL,
  txdb_transcript = NULL
)
```
**Arguments**

**infile**  
the path for the input file for the mutation data of Mutation Position Format.

**numBases**  
the number of upstream and downstream flanking bases (including the mutated base) to take into account.

**trDir**  
the index representing whether transcription direction is considered or not. The gene annotation information is given by UCSC knownGene (TxDb.Hsapiens.UCSC.hg19.knownGene object) When trDir is TRUE, the mutations located in intergenic region are excluded from the analysis.

**bs_genome**  
this argument specifies the reference genome (e.g., B Sgenome.Mmusculus.UCSC.mm10 can be used for the mouse genome). See https://bioconductor.org/packages/release/bioc/html/BSgenome.html for the available genome list

**txdb_transcript**  
this argument specified the transcript database (e.g., TxDb.Mmusculus.UCSC.mm10.knownGene can be used for the mouse genome). See https://bioconductor.org/packages/release/bioc/html/AnnotationDbi.html for details.

**Value**

The output is an instance of MutationFeatureData S4 class (which stores summarized information on mutation data). This will be typically used as the initial values for the global test and the local test.

**Examples**

```r
inputFile <- system.file("extdata/esophageal.mp.txt.gz", package="HiLDA")
G <- hildaReadMPFile(inputFile, numBases=5, trDir=TRUE)
```

---

**hildaRhat**  
*Output the maximum potential scale reduction statistic of all parameters estimated*

**Description**

Output the maximum potential scale reduction statistic of all parameters estimated.

**Usage**

`hildaRhat(jagsOutput)`

**Arguments**

**jagsOutput**  
the output jags file generated by the jags function from the R2jags package.
Value

a number for the Rhat statistic.

Examples

```r
inputFile <- system.file("extdata/hildaLocal.rdata", package="HiLDA")
hildaLocal <- readRDS(inputFile)
hildaRhat(hildaLocal)
```

---

**hildaTest**

*Apply HiLDA to statistically testing the global difference in burdens of mutation signatures between two groups*

**Description**

Apply HiLDA to statistically testing the global difference in burdens of mutation signatures between two groups

**Usage**

```r
hildaTest(
  inputG, 
  numSig, 
  refGroup, 
  useInits = NULL, 
  sigOrder = NULL, 
  nIter = 2000, 
  nBurnin = 0, 
  pM1 = 0.5, 
  localTest = TRUE, 
  ...
)
```

**Arguments**

- **inputG** a MutationFeatureData S4 class output by the pmsignature.
- **numSig** an integer number of the number of mutational signatures.
- **refGroup** the indice indicating the samples in the reference group.
- **useInits** a EstimatedParameters S4 class output by the pmsignature (default: NULL)
- **sigOrder** the order of the mutational signatures.
- **nIter** number of total iterations per chain (default: 2000).
- **nBurnin** length of burn (default: 0).
- **pM1** the probability of sampling the null (default: 0.5)
- **localTest** a logical value (default: TRUE)
- **...** Other arguments passed on to methods.
**MetaInformation-class**

An S4 class to represent a mutation meta information common to many data types

**Description**

@slot type type of data format (independent, full, custom) @slot flankingBasesNum the number of flanking bases to consider (only applicable for independent and full types) @slot transcriptionDirection the flag representing whether transcription direction is considered or not @slot possibleFeatures a vector representing the numbers of possible values for each mutation feature

---

**MutationFeatureData-class**

An S4 class representing the mutation data

**Description**

An S4 class representing the mutation data

**Slots**

featureVectorList a list of feature vectors actually observed in the input mutation data
sampleList a list of sample names observed in the input mutation data
countData a matrix representing the number of mutations and samples. The (1st, 2nd, 3rd) columns are for (mutation pattern index, sample index, frequencies).
mutationPosition a data frame containing position and mutations
mySquareEM

*Description*

A function for estimating parameters using Squared EM algorithm

*Usage*

```r
mySquareEM(p, y, tol = 1e-04, maxIter = 10000)
```

*Arguments*

- `p`: this variable includes the parameters for mutation signatures and membership parameters
- `y`: this variable includes the information on the mutation features, the number of mutation signatures specified and so on
- `tol`: tolerance for the estimation (when the difference of log-likelihoods become below this value, stop the estimation)
- `maxIter`: the maximum number of iteration of estimation

*Value*

a list

---

pmBarplot

*Description*

Plot both mutation signatures and their mutational exposures from pm-signature output

*Usage*

```r
pmBarplot(
  inputG, inputParam, sigOrder = NULL, refGroup = NULL,
  sortSampleNum = TRUE, refName = "Control", altName = "Case",
  charSize = 3
)
```
pmgetSignature

Obtain the parameters for mutation signatures and memberships

pmgetSignature(  
    mutationFeatureData,  
    K,  
    numInit = 10,  
    tol = 1e-04,  
    maxIter = 10000  
)
Arguments

mutationFeatureData
the mutation data (MutationFeatureData class (S4 class)) by the hildaReadMPFile.

K
the number of mutation signatures

numInit
the number of performing calculations with different initial values

tol
tolerance for the estimation (when the difference of log-likelihoods become below this value, stop the estimation)

maxIter
the maximum number of iteration of estimation

Value

The output is an instance of EstimatedParameters S4 class, which stores estimated parameters and other meta-information, and will be used for saving parameter values and visualizing the mutation signatures and memberships

Examples

## After obtaining G (see e.g., hildaReadMPFile function)
load(system.file("extdata/sample.rdata", package="HiLDA"))
Param <- pmgetSignature(G, K = 3)

pmMultiBarplot
    Plot both mutation signatures and their mutational exposures from pm-
signature output for more than two groups

Description

Plot both mutation signatures and their mutational exposures from pmsignature output for more than two groups

Usage

pmMultiBarplot(
  inputG,
  inputParam,
  sigOrder = NULL,
  groupIndices,
  sortSampleNum = TRUE,
  charSize = 3
)
pmPlotSignature

Arguments

- `inputG`: a MutationFeatureData S4 class output by the pmsignature.
- `inputParam`: a estimatedParameters S4 class output by the pmsignature.
- `sigOrder`: the order of signatures if needed (default: NULL).
- `groupIndices`: a vector of group indicators.
- `sortSampleNum`: an indictor variable on whether samples are sorted by the number of mutations (default: TRUE).
- `charSize`: the size of the character on the signature plot (default: 3)

Value

a list of the signature plot and the mean difference plot.

Examples

```r
load(system.file("extdata/sample.rdata", package="HiLDA"))
Param <- pmgetSignature(G, K = 3)

pmPlots <- pmMultiBarplot(G, Param, groupIndices=c(1, rep(2,3), rep(3,6)))
cowplot::plot_grid(pmPlots$sigPlot, pmPlots$propPlot, rel_widths = c(1,3))
```

pmPlotSignature

Plot mutation signatures from pmsignature output

Description

Plot mutation signatures from pmsignature output

Usage

```r
pmPlotSignature(inputParam, sigOrder = NULL, colorList = NULL, ...)
```

Arguments

- `inputParam`: a estimatedParameters S4 class output by the pmsignature.
- `sigOrder`: the order of signatures if needed (default: NULL).
- `colorList`: a list of color to highlight the signatures (default: NULL).
- `...`: additional arguments passed on to visPMS.

Value

a plot object containing all mutational signatures
Examples

```r
load(system.file("extdata/sample.rdata", package="HiLDA"))
Param <- pmgetSignature(G, K = 3)
pmPlotSignature(Param)
```

---

**PMSboundary**

*Definition:

A functional for generating the function checking the parameter (p) is within the restricted conditions or not

**Usage**

```r
PMSboundary(y)
```

**Arguments**

- **y**
  
  this variable includes the information on the mutation features, the number of mutation signatures specified and so on

**Value**

a functional

---

**updateMstepFQC**

*Definition:

Update the parameter F and Q (M-step in the EM-algorithm)

**Usage**

```r
updateMstepFQC(
  vPatternList,
  vSparseCount,
  nTheta,
  fdim,
  signatureNum,
  sampleNum,
  patternNum,
  samplePatternNum,
  isBackground
)
```
**updatePMSParam**

**Arguments**

- **vPatternList**: The list of possible mutation features (converted to a vector)
- **vSparseCount**: The table showing (mutation feature, sample, the number of mutation) (converted to a vector)
- **nTheta**: The parameters in the distribution
- **fdim**: A vector specifying the number of possible values for each mutation signature
- **signatureNum**: The number of mutation signatures
- **sampleNum**: The number of cancer genomes
- **patternNum**: The number of possible combinations of all the mutation features
- **samplePatternNum**: The number of possible combination of samples and mutation patterns
- **isBackground**: The logical value showing whether a background mutation feature is included or not

**Value**

A vector

---

**Description**

A function for updating parameters using EM-algorithm

**Usage**

`updatePMSParam(p, y)`

**Arguments**

- **p**: This variable includes the parameters for mutation signatures and membership parameters
- **y**: This variable includes the information on the mutation features, the number of mutation signatures specified and so on

**Value**

A value
updateTheta_NormalizedC

Update the auxiliary parameters theta and normalize them so that the summation of each group sums to 1 (E-step), also calculate the current log-likelihood value

Description

Update the auxiliary parameters theta and normalize them so that the summation of each group sums to 1 (E-step), also calculate the current log-likelihood value

Usage

```r
updateTheta_NormalizedC(
  vPatternList,
  vSparseCount,
  vF,
  vQ,
  fdim,
  signatureNum,
  sampleNum,
  patternNum,
  samplePatternNum,
  isBackground,
  vF0
)
```

Arguments

- **vPatternList**: The list of possible mutation features (converted to a vector)
- **vSparseCount**: The table showing (mutation feature, sample, the number of mutation) (converted to a vector)
- **vF**: F (converted to a vector)
- **vQ**: Q (converted to a vector)
- **fdim**: a vector specifying the number of possible values for each mutation signature
- **signatureNum**: the number of mutation signatures
- **sampleNum**: the number of cancer genomes
- **patternNum**: the number of possible combinations of all the mutation features
- **samplePatternNum**: the number of possible combination of samples and mutation patterns
- **isBackground**: the logical value showing whether a background mutation features is included or not
- **vF0**: a background mutation features
visPMS

Description

Generate visualization of mutation signatures for the model with substitution patterns and flanking bases represented by the independent representation.

Usage

```r
visPMS(
  vF,
  numBases,
  baseCol = NA,
  trDir = FALSE,
  charSize = 5,
  isScale = FALSE,
  alpha = 2,
  charLimit = 0.25
)
```

Arguments

- `vF` a matrix for mutation signature
- `numBases` the number of flanking bases
- `baseCol` the colour of the bases (A, C, G, T, plus/minus strand)
- `trDir` the index whether the strand direction is plotted or not
- `charSize` the size of the character
- `isScale` the index whether the height of the flanking base is changed or not
- `alpha` the parameter for the Renyi entropy (applicable only if the isScale is TRUE)
- `charLimit` the limit of char size

Value

a plot of the input mutational signature

Examples

```r
load(system.file("extdata/sample.rdata", package="HiLDA"))
Param <- pmgetSignature(G, K = 3)

sig <- slot(Param, "signatureFeatureDistribution")[1, ,]
visPMS(sig, numBases = 5, isScale = TRUE)
```
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