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cn.mops - Mixture of Poissons for CNV detection in NGS data

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Contents

1	Introduction	3				
2	Getting started and quick start	3				
3	Input of cn.mops: BAM files, GRanges objects, or numeric matrices3.1Read count matrices as input3.2BAM files as input	4 4 5				
4	Copy number estimation with cn.mops 4.1 Running cn.mops 4.2 The result object	6 6 7				
5	Visualization of the result5.1Chromosome plots5.2CNV region plots	9 9 10				
6	Exome sequencing data	11				
7	Cases vs. Control or Tumor vs. Normal	14				
8	Heterosomes and CNVs of tumor samples	14				
9	cn.mops for haploid genomes	16				
10	Adjusting sensitivity, specificity and resolution for specific applications	16				
11	Overview of study designs and cn.mops functions	16				
12	2 Exporting cn.MOPS results in tabular format					
13	How to cite this package	18				

1 Introduction

The cn.mops package is part of the Bioconductor (http://www.bioconductor.org) project. The package allows to detect copy number variations (CNVs) from next generation sequencing (NGS) data sets based on a generative model. Please visit http://www.bioinf.jku.at/ software/cnmops.html for additional information.

To avoid the false discoveries induced by read count variations along the chromosome or across samples, we propose a "Mixture Of PoissonS model for CNV detection" (cn.MOPS). The cn.MOPS model is not affected by read count variations along the chromosome, because at each DNA position a local model is constructed. Read count variations across samples are decomposed by the cn.MOPS model into integer copy numbers and noise by its mixture components and Poisson distributions, respectively. In contrast to existing methods, cn.MOPS model's posterior provides integer copy numbers together with their uncertainty. Model selection in a Bayesian framework is based on maximizing the posterior given the samples by an expectation maximization (EM) algorithm. The model incorporates the linear dependency between average read counts in a DNA segment and its copy number. Most importantly, a Dirichlet prior on the mixture components prefers constant copy number 2 for all samples. The more the data drives the posterior away from the Dirichlet prior corresponding to copy number two, the more likely the data is caused by a CNV, and, the higher is the informative/non-informative (I/NI) call. cn.MOPS detects a CNV in the DNA of an individual as a segment with high I/NI calls. I/NI call based CNV detection guarantees a low false discovery rate (FDR) because wrong detections are less likely for high I/NI calls. We assume that the genome is partitioned into segments in which reads are counted but which need not be of constant length throughout the genome. For each of such an segment we build a model. We consider the read counts x at a certain segment of the genome, for which we construct a model across samples. The model incorporates both read count variations due to technical or biological noise and variations stemming from copy number variations. For further information regarding the algorithm and its assessment see the cn.MOPS homepage at http://www.bioinf.jku.at/software/cnmops/cnmops.html.

2 Getting started and quick start

To load the package, enter the following in your R session:

> library(cn.mops)

The whole pipeline will only take a few steps, if BAM files are available (for read count matrices directly go to step 2):

- 1. Getting the input data from BAM files (also see Section 3.2 and Section 3).
 - > BAMFiles <- list.files(pattern=".bam\$")</pre>
 - > bamDataRanges <- getReadCountsFromBAM(BAMFiles)</pre>
- 2. Running the algorithm (also see Section 4.2).

> res <- cn.mops(bamDataRanges)</pre>

- 3. Visualization of the detected CNV regions. For more information about the result objects and visualization see Section 4.2.
 - > plot(res,which=1)



3 Input of cn.mops: BAM files, GRanges objects, or numeric matrices

3.1 Read count matrices as input

cn.mops does not require the data samples to be of any specific kind or structure. cn.mops only requires a *read count matrix*, i.e., given N data samples and m genomic segments, this is an $m \times N$ real- or integer-valued matrix **X**, in which an entry x_{ij} corresponds to the read count of sample j in the *i*-th segment. E.g. in the following read count matrix sample three has 17 reads in the second segment: $x_{23} = 71$.

		Sar	nple 1	Sample 2	Sample 3	Sampl	le 4
	Segment 1	(88	82	79	101	
	Segment 2		83	78	71	99	
v _	Segment 3		43	50	55	37	
$\mathbf{\Lambda} =$	Segment 4		47	58	48	42	
	Segment 5		73	86	95	91	
	Segment 6		92	90	80	71)

cn.mops can handle numeric and integer matrices or GRanges objects, in which the read counts are stored as values of the object.

3.2 BAM files as input

The most widely used file format for aligned short reads is the Sequence Alignment Map (SAM) format or in the compressed form the Binary Alignment Map (BAM). We provide a simple function that makes use of the Rsamtools package to obtain the alignment positions of reads. The result object of the function can directly be used as input for cn.mops. The author can provide functions for input formats other than BAM upon request: *cn.mops@bioinf.jku.at*.

```
> BAMFiles <- list.files(system.file("extdata", package="cn.mops"),pattern=".bam$",
+ full.names=TRUE)
> bamDataRanges <- getReadCountsFromBAM(BAMFiles,
+ sampleNames=paste("Sample",1:3))
```

In bamDataRanges you have now stored the genomic segments (left of the |'s) and the read counts (right of the |'s):

```
> (bamDataRanges)
```

GRanges	object	wit:	h 2522	ranges	and	3 metad	lat	ta columns:	:	
	seqnam	nes		ra	nges	strand		Sample 1	Sample 2	Sample 3
	<r1< td=""><td>.e></td><td></td><td><iran< td=""><td>ges></td><td><rle></rle></td><td></td><td><integer></integer></td><td><integer></integer></td><td><integer></integer></td></iran<></td></r1<>	.e>		<iran< td=""><td>ges></td><td><rle></rle></td><td></td><td><integer></integer></td><td><integer></integer></td><td><integer></integer></td></iran<>	ges>	<rle></rle>		<integer></integer>	<integer></integer>	<integer></integer>
[1]		20		1-2	5000	*		0	0	0
[2]		20	:	25001-5	0000	*		0	0	0
[3]		20	!	50001-7	5000	*		762	848	784
[4]		20	7	5001-10	0000	*		0	0	0
[5]		20	100	0001-12	5000	*	I	0	0	0
• • •	•	••			• • •	• • •	•		• • •	
[2518]		20	629250	01-6295	0000	*		0	0	0
[2519]		20	6295000	01-6297	5000	*		0	0	0
[2520]		20	6297500	01-6300	0000	*		0	0	0
[2521]		20	630000	01-6302	5000	*		0	0	0
[2522]		20	630250	01-6302	5520	*		0	0	0

seqinfo: 1 sequence from an unspecified genome

4 Copy number estimation with cn.mops

To get a first impression, we use a data set, in which CNVs have been artificially implanted. The simulated data set was generated using distributions of read counts as they appear in real sequencing experiments. CNVs were implanted under the assumption that the expected read count is linear dependent on the copy number. For example in a certain genomic we expect λ reads for copy number 2, then we expect 2λ reads for copy number 4. The linear relationship was confirmed in different studies, like Alkan *et al.* (2009), Chiang *et al.* (2008) and Sathirapongsasuti *et al.* (2011).

4.1 Running cn.mops

The read counts are stored in the objects X and XRanges, which are the two basic input types that cn.mops allows:

```
> data(cn.mops)
> ls()
```

[1]	"BAMFiles"	"CNVRanges"	"X"	"XRanges"
[5]	"bamDataRanges"	"cn.mopsVersion"	"exomeCounts"	"resCNMOPS"

The same data is stored in a GRanges object, in which we see the genomic coordinates, as well as the read counts (values):

```
> head(XRanges[,1:3])
```

GRanges	object	with 6	ranges	and 3	me	tadata	colu	mns:	
S	eqnames		ranges	stran	.d		S_1	S_2	S_3
	<rle></rle>	<i]< td=""><td>Ranges></td><td><rle< td=""><td>> </td><td><integ< td=""><td>ger></td><td><integer></integer></td><td><integer></integer></td></integ<></td></rle<></td></i]<>	Ranges>	<rle< td=""><td>> </td><td><integ< td=""><td>ger></td><td><integer></integer></td><td><integer></integer></td></integ<></td></rle<>	>	<integ< td=""><td>ger></td><td><integer></integer></td><td><integer></integer></td></integ<>	ger>	<integer></integer>	<integer></integer>
[1]	chrA		1-25000		*		102	93	109
[2]	chrA	2500	1-50000		*		118	99	100
[3]	chrA	5000	1-75000		*		85	81	82
[4]	chrA	75001	-100000		*		87	116	106
[5]	chrA	100001	-125000		*		87	68	89
[6]	chrA	125001	-150000		*		87	91	91
seqin:	fo: 1 se	equence	from an	n unsp	eci	fied g	enome	; no seqle	engths

sequinto. I sequence from an unspectified genome, no sequenge

We are now ready to run cn.mops on the GRanges object:

```
> resCNMOPS <- cn.mops(XRanges)</pre>
```

To calculate integer copy number use the command calcIntegerCopyNumbers:

> resCNMOPS <- calcIntegerCopyNumbers(resCNMOPS)</pre>

6

Alternatively, it is possible to use an integer matrix, in which the genomic coordinates can be stored as rownames and the entries are the read counts. For example the data from above represented by an integer matrix X:

> head(X[,1:3])

```
S_1 S_2 S_3
Chr_A_1_25000
                    102 93 109
Chr_A_25001_50000
                    118 99 100
Chr_A_50001_75000
                            82
                    85
                        81
Chr_A_75001_100000
                    87 116 106
Chr_A_100001_125000
                    87
                        68
                            89
Chr_A_125001_150000 87
                        91 91
```

We are now ready to run cn.mops on the integer matrix:

```
> resCNMOPSX <- cn.mops(X)</pre>
```

To calculate integer copy number use the command calcIntegerCopyNumbers:

```
> resCNMOPSX <- calcIntegerCopyNumbers(resCNMOPSX)</pre>
```

Note that the two results resCNMOPS and resCNMOPSRanges identify the same CNVs:

```
> all(individualCall(resCNMOPSX)==individualCall(resCNMOPS))
```

4.2 The result object

To get a summary of the CNV detection result, just enter the name of the object (which implicitly calls show):

> (resCNMOPS)

The CNVs per individual are stored in the slot cnvs:

```
> cnvs(resCNMOPS)[1:5]
```

GRanges object with 5 ranges and 4 metadata columns:

	seqnames	ranges	strand		sampleName	median
	<rle></rle>	<iranges></iranges>	<rle></rle>		<character></character>	<numeric></numeric>
[1]	chrA	1775001-1850000	*		S_1	-1.00000
[2]	chrA	53300001-53400000	*	I	S_1	-5.32193
[3]	chrA	113175001-113325000	*		S_1	-0.99991
[4]	chrA	48575001-48650000	*		S_2	-5.32193
[5]	chrA	70625001-70750000	*		S_2	-5.32193
	mear	n CN				

<numeric> <character>
[1] -0.999999 CN1
[2] -5.321928 CN0
[3] -0.999682 CN1
[4] -5.321928 CN0
[5] -5.321928 CN0
-----seqinfo: 1 sequence from an unspecified genome; no seqlengths

Segments, in which individual CNVs accumulate, are called CNV regions and can be accessed by cnvr:

> cnvr(resCNMOPS)[1,1:5] GRanges object with 1 range and 5 metadata columns: seqnames ranges strand | S_1 S_2 <Rle> <IRanges> <Rle> | <character> <character> [1] chrA 1775001-1850000 * CN1 CN2 S_5 S 3 S 4 <character> <character> <character> CN2 CN2 CN2 [1] seqinfo: 1 sequence from an unspecified genome; no seqlengths

We now want to check, whether cn.mops found the implanted CNVs. We have stored the implanted CNVs (see beginning of Section) in the object CNVRanges.

```
> (CNVRanges[15,1:5])
```

GRanges object with 1 range and 5 metadata columns: seqnames ranges strand S 1 S_2 S 3 <Rle> <IRanges> <Rle> | <integer> <integer> <integer> chrA 1751017-1850656 [1] * | 1 2 2 S 4 S 5 <integer> <integer> 2 2 [1] _____ seqinfo: 1 sequence from an unspecified genome; no seqlengths

Next we identify overlaps between CNVs that were detected by cn.mops and CNVs that were implanted. Towards this end we use the functions of the GenomicRanges package.

> ranges(cnvr(resCNMOPS))[1:2]

> ranges(cnvr(resCNMOPS)) %over% ranges(CNVRanges)

The detected CNV regions all overlap with the known CNV regions contained in CNVRanges.

The function cn.mops creates an instance of the S4 class CNVDetectionResult that is defined by the present package. To get detailed information on which data are stored in such objects, enter

> help(CNVDetectionResult)

5 Visualization of the result

5.1 Chromosome plots

cn.mops allows for plotting the detected segments of an individual at one chromosome by a plot similar to the ones produced by DNAcopy:

> segplot(resCNMOPS,sampleIdx=13)

S_13



Chromosome chrA

Figure 1: The x-axis represents the genomic position and on the y-axis we see the log ratio of the read counts (green) and the copy number call of each segment (red).

5.2 CNV region plots

cn.mops allows for plotting the detected CNV regions:

> plot(resCNMOPS,which=1)



Figure 2: The x-axis represents the genomic position and on the y-axis we see the read counts (left), the call of the local model (middle) and the CNV call produced by the segmentation algorithm. Blue lines mark samples having a copy number loss.

6 Exome sequencing data

To apply cn.mops to exome sequencing data requires a different preprocessing, since constant windows spanning the whole genome are not appropiate. The initial segments in which the reads are counted should be chosen as the regions of the baits, targets or exons. The read count matrix can now be generated by using the function getSegmentReadCountsFromBAM that requires the genomic coordinates of the predefined segments as GRanges object. The resulting read count

matrix can directly be used as input for cn.mops. A possible processing script could look like the following:

```
> library(cn.mops)
> BAMFiles <- list.files(pattern=".bam$")</pre>
> segments <- read.table("targetRegions.bed",sep="\t",as.is=TRUE)</pre>
> gr <- GRanges(segments[,1], IRanges(segments[,2], segments[,3]))</pre>
> X <- getSegmentReadCountsFromBAM(BAMFiles,GR=gr)</pre>
> resCNMOPS <- exomecn.mops(X)</pre>
```

> resCNMOPS <- calcIntegerCopyNumbers(resCNMOPS)</pre>

We included an exome sequencing data set in this package. It is stored in exomeCounts.

```
> resultExomeData <- exomecn.mops(exomeCounts)</pre>
> resultExomeData <- calcIntegerCopyNumbers(resultExomeData )</pre>
```

> plot(resultExomeData,which=5)

12



Figure 3: ExomeSeq data results.

Possible issues and notes A problem can occur, if the names of the reference sequences, e.s. chromosomes, are inconsistent between the bed file and the bam file. For example "chr1", "chr2",...,"chrX","chrY" and "1","2",...,"X","Y". This can easily be solved by replacing the seqlevels of the GRanges object:

```
> #the following removes the "chr" from reference sequence names
```

```
> library(GenomeInfoDb)
```

> seqlevels(gr) <- gsub("chr","",seqlevels(gr))</pre>

Results can also be improved if you extend your target regions by a small amount of bases to the left and to the right (in the following case it is 30bp):

```
> gr <- GRanges(segments[,1], IRanges(segments[,2]-30, segments[,3]+30))
> gr <- reduce(gr)</pre>
```

7 Cases vs. Control or Tumor vs. Normal

For detection of CNVs in a setting in which the normal state is known, the function referencecn.mops can be applied. It implements the cn.MOPS algorithm adjusted to this setting. For tumor samples very high copy numbers can be present – the maximum copy number with the default setting is 8 – and cn.mops has to be adjusted to allow higher copy numbers.

```
> resRef <- referencecn.mops(cases=X[,1],controls=rowMeans(X),</pre>
                  classes=c("CNO", "CN1", "CN2", "CN3", "CN4", "CN5", "CN6",
+
                                   "CN7", "CN8", "CN16", "CN32", "CN64", "CN128"),
+
                  I = c(0.025, 0.5, 1, 1.5, 2, 2.5, 3, 3.5, 4, 8, 16, 32, 64),
+
                  segAlgorithm="DNAcopy")
+
Analyzing: Sample.1
> resRef <- calcIntegerCopyNumbers(resRef)</pre>
> (cnvs(resRef))
GRanges object with 4 ranges and 4 metadata columns:
                  ranges strand | sampleName
      seqnames
                                                  median
                                                               mean
         <Rle> <IRanges> <Rle> | <character> <numeric> <numeric>
  [1]
         undef 2029-2032
                               *
                                        Case_1 0.584963
                                                            0.5850
  [2]
         undef 2133-2136
                                        Case_1 -5.321928
                               *
                                                            -5.3219
                                        Case_1 -2.660964
                                                            -2.6610
  [3]
         undef 4051-4054
                               *
  [4]
         undef 4528-4533
                               *
                                        Case_1 -1.000000
                                                            -1.0000
               CN
      <character>
  [1]
              CN3
              CNO
  [2]
  [3]
              CN1
  [4]
              CN1
  seqinfo: 1 sequence from an unspecified genome; no seqlengths
```

8 Heterosomes and CNVs of tumor samples

With the default settings the normalization procedure assumes that the ploidy of each sample is the same. However, it is possible to account for different karyotypes. When analyzing CNVs on the X or Y chromosome one possibility is to treat males and females separately. The second option is to provide the normalization function with the information about the gender, that is different

ploidy states of the X and Y chromosome. This can be handled by the ploidy parameter of the normalization function. In the following we show the normalization for the X chromosome, if the first 10 individuals are males (ploidy set to 1) and the next 30 individuals are females (ploidy set to 2):

> XchrX <- normalizeChromosomes(X[1:500,],ploidy=c(rep(1,10),rep(2,30)))
> cnvr(calcIntegerCopyNumbers(cn.mops(XchrX,norm=FALSE)))

Range	es object wit	th 1 range an	nd 40 metadat	ta columns:		
	seqnames	ranges stra	nd	S_1	S_2	S_3
	<rle> <ih< td=""><td>Ranges> <rle< td=""><td>e> <charact< td=""><td>cer> <charac< td=""><td>ter> <charact< td=""><td>ter></td></charact<></td></charac<></td></charact<></td></rle<></td></ih<></rle>	Ranges> <rle< td=""><td>e> <charact< td=""><td>cer> <charac< td=""><td>ter> <charact< td=""><td>ter></td></charact<></td></charac<></td></charact<></td></rle<>	e> <charact< td=""><td>cer> <charac< td=""><td>ter> <charact< td=""><td>ter></td></charact<></td></charac<></td></charact<>	cer> <charac< td=""><td>ter> <charact< td=""><td>ter></td></charact<></td></charac<>	ter> <charact< td=""><td>ter></td></charact<>	ter>
[1]	undef	1-500	*	CN1	CN1	CN1
	S_4	S_5	S_6	S_7	S_8	
	<character></character>	<character></character>	<character></character>	<character></character>	<character></character>	
[1]	CN1	CN1	CN1	CN1	CN1	
	S_9	S_10	S_11	S_12	S_13	
	<character></character>	<character></character>	<character></character>	<character></character>	<character></character>	
[1]	CN1	CN1	CN2	CN1	CN2	
	S_14	S_15	S_16	S_17	S_18	
	<character></character>	<character></character>	<character></character>	<character></character>	<character></character>	
[1]	CN2	CN1	CN2	CN1	CN2	
	S_19	S_20	S_21	S_22	S_23	
	<character></character>	<character></character>	<character></character>	<character></character>	<character></character>	
[1]	CN2	CN2	CN2	CN2	CN2	
	S_24	S_25	S_26	S_27	S_28	
	<character></character>	<character></character>	<character></character>	<character></character>	<character></character>	
[1]	CN2	CN2	CN2	CN1	CN1	
	S_29	S_30	S_31	S_32	S_33	
	<character></character>	<character></character>	<character></character>	<character></character>	<character></character>	
[1]	CN2	CN2	CN2	CN2	CN2	
	S_34	S_35	S_36	S_37	S_38	
	<character></character>	<character></character>	<character></character>	<character></character>	<character></character>	
[1]	CN2	CN2	CN2	CN2	CNO	
	S_39	S_40				
	<character></character>	<character></character>				
[1]	CN2	CN1				
		_				
seq:	info: 1 seque	ence from an	unspecified	genome; no s	seqlengths	

Karyotype information can also improve results of CNV detection in tumor samples. The best results can be reached, if for each chromosome the number of appearances in the cell is known. In this case normalization should be applied to each chromosome separately.

9 cn.mops for haploid genomes

For haploid genomes the prior assumption is that all samples have copy number 1. The function haplocn.mops implements the cn.MOPS algorithm adjusted to haploid genomes.

> resHaplo <- haplocn.mops(X)
</pre>

> resHaplo <- calcIntegerCopyNumbers(resHaplo)</pre>

10 Adjusting sensitivity, specificity and resolution for specific applications

The default parameters of both the local models of cn.mops and the segmentation algorithm were optimized on a wide ranged of different data sets. However, you might want to adjust sensitivity and specificity or resolution to your specific needs.

- upperThreshold The calling threshold for copy number gains, a positive value. Lowering the threshold will increase the detections, raising will decrease the detections.
- lowerThreshold The calling threshold for copy number losses, a negative value. Raising the threshold will increase the detections, lowering will decrease the detections.
 - priorImpact This parameter should be optimized for each data set, since it is influenced by number of samples as well as noise level. The higher the value, the more samples will have copy number 2, and consequently less CNVs will be detected.
 - minWidth The minimum length of CNVs measured in number of segments. The more adjacent segments with a high or low copy number call are joined, the higher the confidence in the detections. A lower value will lead to more shorter segments, and a higher value will yield to less, but longer segments.

The length of the initial segments is also crucial. They should be chosen such that on average 50 to 100 reads lie in one segment. The WL parameter of getReadCountsFromBAM determines this resolution.

11 Overview of study designs and cn.mops functions

In Table1 we give an overview of the functions implemented in this package and present settings for which they are appropriate. All these functions work for multiple, at least two, samples.CNV detection for single samples usually yields many false detections, because of characteristics of genomic segments that lead to a higher or lower read count (and coverage). These biases can usually not be corrected for (except for the GC content and the mappability bias). Being aware of all these problems we have implemented the function singlecn.mops for cases in which only one sample is available.

Seq. Type	Ploidy	Study	Samples	Function
WGS	2n	cohort/non-tumor/GWAS	≥ 5	cn.mops
WGS	2n	tumor vs. normal	≥ 2	referencecn.mops
ES	2n	cohort/non-tumor/GWAS	≥ 5	exomecn.mops
ES	2n	tumor vs. normal	≥ 2	referencecn.mops
WGS	1n	cohort/non-tumor/GWAS	≥ 5	haplocn.mops
WGS	1n	tumor vs. normal	≥ 2	not implemented
ES	1n	cohort/non-tumor/GWAS	≥ 5	haplocn.mops
ES	1n	tumor vs. normal	≥ 2	not implemented

Table 1: Seq. Type reports the sequencing technology that was used: whole genome sequencing (WGS) or targeted/exome sequencing (ES). Ploidy gives the usual ploidy of the samples. In case of a tumor vs. control study the control sample is meant. Study: The type of study to be analyzed for CNVs: either a cohort study, such the HapMap or the 1000Genomes Project, or studies including a number of non-tumor samples or studies with both healthy and diseased individuals, i.e. genome wide association studies (GWAS). Samples reports the minimum number of samples needed for the analysis. Function gives the function of the cn.mops package that is appropriate for this setting.

12 Exporting cn.MOPS results in tabular format

Users can extract the segmentation, the CNVs and the CNV regions with the following:

```
> library(cn.mops); data(cn.mops)
> result <- calcIntegerCopyNumbers(cn.mops(XRanges))
> segm <- as.data.frame(segmentation(result))
> CNVs <- as.data.frame(cnvs(result))
> CNVRegions <- as.data.frame(cnvr(result))</pre>
```

The results can be exported with write.csv for Excel, LibreOffice Calc, etc. These files will include the genomic position, copy number and other information.

```
> write.csv(segm,file="segmentation.csv")
> write.csv(CNVs,file="cnvs.csv")
> write.csv(CNVRegions,file="cnvr.csv")
```

13 How to cite this package

If you use this package for research that is published later, you are kindly asked to cite it as follows: (Klambauer *et al.*, 2012).

To obtain BibTEX entries of the reference, you can enter the following into your R session:

> toBibtex(citation("cn.mops"))

References

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