## GWAS-based Mendelian Randomization Path Analysis

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#### Abstract

GMRP can perform analyses of Mendelian randomization (MR), correlation, path of causal variables onto disease of interest and SNP annotation analysis. MR includes SNP selection with given criteria and regression analysis of causal variables on the disease to generate beta values of causal variables on the disease. Using the beta vectors, GMRP performs correlation and path analyses to construct path diagrams of causal variables to the disease. GMRP consists of 8 R functions: chrp,fmerge,mktable,pathdiagram,pathdiagram2,path,snpPositAn not, ucs cannot and 5 datasets: beta.data,cad.data,lpd.data,SNP358.data,SNP368annot.data. chrp is used to separate string vector hg19 into two numeric vectors: chromosome number and SNP chromosome position. Function fmerge is used to merge two GWAS result datasets into one dataset. Function mktable performs SNP selection and creates a standard beta table for function path to do MR and path analyses. Function pathdiagram is used to create a path diagram of causal variables onto a given disease or onto outcome. Function pathdiagram2 can merge two-level pathdiagrams into one nested pathdiagram where inner pathdiagram is a pathdiagram of causal variables contributing to outcome and the outside pathdiagram is a path diagram of causal variables including outcome onto the disease. The five datasets provide examples for running these functions. lpd.data and cad.data provide an example to create a standard beta dataset for path function to do path analysis and SNP data for SNP annotation analysis by performing mktable and fmerge. beta.data are a standard beta dataset for path analysis. SNP358.data provide an example for snpPositAnnot to do SNP position annotation analysis and SNP368annot.data are for ucscannot to perform SNP function annotation analysis.

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#### 1 Introduction

As an example of human disease, coronary artery disease (*CAD*) is one of the causes leading to death and infirmity worldwide [1]. Low-density lipoprotein cholesterol (*LDL*) and triglycerides (*TG*) are viewed as risk factors causing *CAD*. In epidemiological studies, plasma concentrations of increasing *TG* and *LDL* and deceasing high-density lipoprotein cholesterol (*HDL*) have been observed to be associated with risk for *CAD* [2, 3]. However, from observational studies, one could not directly infer that these cholesterol concentrations in plasma are risk factors causing *CAD* [4, 3, 5, 6]. A big limitation of observational studies is to difficultly distinguish between causal and spurious associations due to confounding [7]. An efficient approach to overcome this limitation is *Mendelian Randomization* (*MR*) analysis [5, 8] where genetic variants are used as instrumental variables. For this reason, many investigators tried to use genetic variants to assess causality and estimate the causal effects on the diseases.

MR analysis can perfectly exclude confounding factors associated with disease. However, when we expand one causal variable to many, MR analysis becomes challenged and complicated because the genetic variant would have additional effects on the other risk factors, which violate assumption of no pleiotropy. An unknown genetic variant in MR analysis possibly provides a false instrument for causal effect assessment of risk factors on the disease. The reason is that if this genetic variant is in LD with another gene that is not used but has effect on the disease of study [5, 9]. It then violates the third assumption. These two problems can be addressed by using multiple instrumental variables. For this reason, Do et al (2013)developed statistic approach to address this issue [4]. However, method of Do et al [4] cannot disentangle correlation effects among the multiple undefined risk factors on the disease of study. The beta values obtained from regression analyses are not direct causal effects because their effects are entangled with correlations among these undefined risk factors.

The best way to address the entanglement of multiple causal effects is path analysis that was developed by Wright [12, 11]. This is because path analysis can dissect beta values into direct and indirect effects of causal variables on the disease. However, path analysis has not broadly been applied to diseases because diseases are usually binary variable. The method of Do [4] makes it possible to apply path analysis to disentangle causal effects of undefined risk factors on diseases. For doing so, we here provide **R package** *GMRP* (*GWAS*-based *MR* and *path analysis*) to solve the above issues.

This vignette is intended to give a rapid introduction to the commands used in implementing MR analysis, regression analysis, and path analysis, including SNP annotation and chromosomal position analysis by means of the GMRP package.

We assume that user has the *GWAS* result data from *GWAS* analysis or *GWAS* meta analysis of *SNP*s associated with risk or confounding factors and a disease of study. If all studied causal variables of *GWAS* data are separately saved in different sheet files, then files are assumed to have the same sheet format and they are required to be merged by using function fmerge into one sheet file without disease *GWAS* data. After a standard beta table is created

with mktable, user can use function path to perform *RM* and path analyses. Using the result of path analysis, user can draw path plot(*pathdiagram*) with functions pathdiagram and pathdiagram2. These will be introduced in detail in the following examples.

We begin by loading the GMRP package.

> library(GMRP)

#### 2 Loading Data

*GMRP* provides five data files:beta.data, cad.data, lpd.data, SNP358.data and SNP368annot.data where

Lpd.data was a subset (1069 SNPs) of four GWAS result datasets for LDL, HDL, TG and TC. These GWAS result data sheets were downloaded from the website<sup>1</sup> where there are 120165 SNPs on 23 chromosomes and 40 variables. Four GWAS result datasets for LDL, HDL, TG and TC were merged into one data sheet by using fmerge (fl1,fl2,ID1,ID2,A,B,method) where fl1 and fl2 are two GWAS result data sheets. ID1 and ID2 are key *id* in files fl1 and fl2, respectively, and required. A and B are respectily postfix for fl1 and fl2. Default values are A="" and B="". *method* is method for merging . In the current version, there are four methods: *method*="No" or "NO" or "N" or "n" means that the data with unmatched SNPs in file1 and file 2 are not saved in the merged file; *method*="ALL" or "All" or "all" or "A" or "a" indicates that the data with all unmatched SNPs in file 1 and file 2 are saved in the unpaired way in the merged data file; If *method*="file1", then those with unmatched SNPs only from file1 are saved or if *method*="file2", fmerge will save the data with unmatched SNPs only from file2". Here is a simple example:

```
> data1 <- matrix(NA, 20, 4)</pre>
> data2 <- matrix(NA, 30, 7)</pre>
> SNPID1 <- paste("rs", seq(1:20), sep="")</pre>
> SNPID2 <- paste("rs", seq(1:30), sep="")</pre>
> data1[,1:4] <- c(round(runif(20), 4), round(runif(20), 4), round(runif(20), 4), round(runif(20), 4))
> data2[,1:4] <- c(round(runif(30), 4), round(runif(30), 4), round(runif(30), 4), round(runif(30), 4))</pre>
> data2[,5:7] <- c(round(seq(30)*runif(30), 4), round(seq(30)*runif(30), 4), seq(30))</pre>
> data1 <- cbind(SNPID1, as.data.frame(data1))</pre>
> data2 <- cbind(SNPID2, as.data.frame(data2))</pre>
> dim(data1)
> dim(data2)
> colnames(data1) <- c("SNP", "var1", "var2", "var3", "var4")</pre>
> colnames(data2) <- c("SNP", "var1", "var2", "var3", "var4", "V1", "V2", "V3")</pre>
> data1<-DataFrame(data1)</pre>
> data2<-DataFrame(data2)</pre>
> data12 <- fmerge(fl1=data1, fl2=data2, ID1="SNP", ID2="SNP", A=".dat1", B=".dat2", method="No")</pre>
```

User can take the following approach to merge all four lipid files into a data sheet: LDLHDL<fmerge(fl1=LDLfile,fl2=HDLfile, ID1="SNP", ID2="SNP", A=".LDL", B=".HDL", method="No")

TGTC<-fmerge(fl1=TGfile,fl2=TCfile, ID1="SNP", ID2="SNP", A=".TG", B=".TC", method="No")

*lpd<-fmerge(fl1=LDLHDL,fl2=TGTC,ID1="SNP",ID2="SNP",A="",B="",method="No")* 

cad.data was also a subset (1069 SNPs) of original GWAS meta-analyzed dataset that was downloaded from the website<sup>2</sup> and contains 2420360 *SNP*s and 12 variables.

<sup>2</sup>http://www. cardiogramplusc4d.org/ downloads/

<sup>1</sup>http://csg.sph.umich. edu//abecasis/public/

lipids2013/

beta.data that was created by using function mktable and fmerge from lpd.data and cad.data is a standard beta table for MR and path analyses.

SNP358.data contains 358 SNPs selected by mktable for SNP position annotation analysis.

SNP368annot.data is the data obtained from function analysis with http://snp-nexus.org/ index.html*SNP* Annotation Tool and provides example of performing function ucscanno to draw a 3D pie and output the results of proportions of *SNP*s coming from gene function various elements.

```
> data(cad.data)
> #cad <- DataFrame(cad.data)</pre>
> cad<-cad.data</pre>
> head(cad)
         SNP
               chr_pos_b36 reference_allele other_allele ref_allele_frequency
                                                                                 pvalue
1 rs3091242 chr1:25547372
                                          С
                                                       Т
                                                                    0.4630502 0.9036396
                                                       Т
2
    rs926438 chr1:25626225
                                          С
                                                                    0.4661719 0.4769371
3 rs11802413 chr1:25633507
                                          С
                                                       Т
                                                                    0.4651288 0.4698333
4 rs7541095 chr1:25633878
                                          С
                                                       Т
                                                                    0.5329650 0.8293105
5 rs10903129 chr1:25641524
                                          G
                                                       А
                                                                    0.5345702 0.3804964
6 rs12746810 chr1:26885720
                                          G
                                                                    0.8749898 0.0945896
                                                       Α
  het_pvalue log_odds log_odds_se N_case N_control model
1 0.90432143 -0.0018321 0.0151330 17085
                                               58384
                                                        FF
2 0.97388037 -0.0098335 0.0138259 21913
                                               62220
                                                        FE
3 0.95992310 -0.0100090 0.0138485 21885
                                               62197
                                                        FE
4 0.83943112 0.0030565 0.0141775 20039
                                               60965
                                                        FE
5 0.95534970 0.0122634
                         0.0139836 21600
                                               59352
                                                        FE
6 0.04893363 -0.0409198
                         0.0244784 19722
                                               60854
                                                        FE
```

> data(lpd.data)

```
> #lpd <- DataFrame(lpd.data)</pre>
```

> lpd<-lpd.data

> head(lpd)

	SNP_hg18.HDL	SNP_hg19.HDL	rsid.HDL A1.HDL	A2.HDL beta.HDL	se.HDL N.H	DL
1	chr19:19379316	chr19:19518316	rs1000237 a	t 0.0083	0.0051 92630.	00
2	chr4:88283455	chr4:88064431	rs10023050 g	a 0.0174	0.0049 92768.	00
3	chr5:156366229	chr5:156433651	rs10036890 t	a 0.0044	0.0062 92644.	98
4	chr19:11085181	chr19:11224181	rs1003723 t	c 0.0051	0.0050 86071.	10
5	chr5:74753409	chr5:74717653	rs10038723 t	c 0.0043	0.0059 92790.	02
6	chr11:116227036	chr11:116721826	rs10047459 t	c 0.0203	0.0070 76329.	02
	P.value.HDL Free	q.A1.1000G.EUR.HDI	L SNP_hg18.LDL	SNP_hg19.LDL	rsid.LDL A1	.LDL
1	0.127300	0.3272	2 chr19:19379316	chr19:19518316	rs1000237	t
2	0.001186	0.4222	2 chr4:88283455	chr4:88064431	rs10023050	а
3	0.551000	0.8417	7 chr5:156366229	chr5:156433651	rs10036890	t
4	0.337800	0.4578	8 chr19:11085181	chr19:11224181	rs1003723	t
5	0.488600	0.2375	5 chr5:74753409	chr5:74717653	rs10038723	t
6	0.013370	0.8074	4 chr11:116227036	chr11:116721826	rs10047459	С
	A2.LDL beta.LDL	se.LDL N.LDL F	P.value.LDL Freq.	A1.1000G.EUR.LDL	SNP_hg18.	TG
1	a 0.0373	0.0054 82988.90	2.755e-11	0.6728	chr19:193793	16
2	g 0.0141	0.0052 83123.00	1.457e-02	0.5778	chr4:882834	55
3	a 0.0245	0.0066 83022.99	3.848e-04	0.8417	chr5:1563662	29
4	c 0.0335	0.0053 77777.00	1.508e-09	0.4578	chr19:110851	81

```
5
          0.0605 0.0063 83135.02
                                   1.381e-19
                                                             0.2375
                                                                     chr5:74753409
          0.0056 0.0073 71581.06
                                   5.302e-01
6
                                                             0.1926 chr11:116227036
      t
     SNP_hq19.TG
                     rsid.TG A1.TG A2.TG beta.TG se.TG
                                                           N.TG P.value.TG
1
  chr19:19518316 rs1000237
                                t
                                      a 0.0368 0.0049 86629.00 2.116e-12
                                      g 0.0293 0.0048 86765.00 2.449e-09
2
   chr4:88064431 rs10023050
                                а
3 chr5:156433651 rs10036890
                                t
                                      a 0.0160 0.0060 86658.99
                                                                 6.558e-03
4
  chr19:11224181 rs1003723
                                t
                                      c 0.0004 0.0048 81143.90
                                                                 8.068e-01
5
   chr5:74717653 rs10038723
                                      c 0.0013 0.0058 86781.02
                                                                 9.066e-01
                                t
6 chr11:116721826 rs10047459
                                с
                                      t 0.0560 0.0066 74837.95 1.523e-14
  Freq.A1.1000G.EUR.TG
                          SNP_hg18.TC
                                          SNP_hg19.TC
                                                          rsid.TC A1.TC A2.TC beta.TC
                0.6728 chr19:19379316 chr19:19518316
                                                        rs1000237
                                                                           a 0.0374
1
                                                                     t
2
                                        chr4:88064431 rs10023050
                0.5778
                        chr4:88283455
                                                                            g
                                                                             0.0162
                                                                     а
3
                0.8417 chr5:156366229 chr5:156433651 rs10036890
                                                                     t
                                                                           а
                                                                              0.0351
4
                0.4578
                       chr19:11085181 chr19:11224181 rs1003723
                                                                     t
                                                                           c 0.0288
5
                0.2375
                        chr5:74753409
                                        chr5:74717653 rs10038723
                                                                     t
                                                                           c 0.0515
6
                0.1926 chr11:116227036 chr11:116721826 rs10047459
                                                                     С
                                                                           t 0.0079
  se.TC
             N.TC P.value.TC Freq.A1.1000G.EUR.TC
1 0.0051 92528.90 1.557e-12
                                          0.6728
2 0.0049 92675.00 1.499e-03
                                          0.5778
3 0.0063 92553.21 3.974e-08
                                          0.8417
4 0.0051 85814.00 1.681e-08
                                          0.4578
5 0.0060 92698.92 4.354e-17
                                          0.2375
6 0.0069 80331.01 2.155e-01
                                          0.1926
```

#### 3 Preparation of Standard Beta Table

The standard beta table for *MR* and path analyses must have the standard format. It has columns: *chrn*, *posit*, *rsid*,  $a1.x_1$ ,  $a1.x_2$ ,  $\cdots$ ,  $a1.x_n$ ,  $freq.x_1$ ,  $freq.x_2$ ,  $\cdots$ ,  $freq.x_n$ ,  $beta.x_1$ ,  $beta.x_2$ ,  $\cdots$ ,  $beta.x_n, sd.x_1$ ,  $sd.x_2$ ,  $\cdots$ ,  $sd.x_n$ ,  $pv_j$ ,  $N.x_1$ ,  $N.x_2$ ,  $\cdots$ ,  $N.x_n$ ,  $pc_j$ , hg.d, SNP.d, freq.d, beta.d, N.d, freq.case,  $pd_j$  where  $x_1, x_2, \cdots, x_n$  are variables.

*beta* is vector of beta values of *SNP*s on variable vector  $X = (x_1, x_2, \cdots, x_n)$ .

*freq* is vector of frequency of allele 1 with respect to variable vector  $X = (x_1, x_2, \cdots, x_n)$ .

sd is vector of standard deviations of variable  $(x_1, x_2, \dots, x_n)$  specific to SNP. If sd does not specifically correspond to SNP, then  $sd.x_i$  has the same value for all SNPs.

d denotes disease.

N is sample size.

*freq.case* is frequency of disease.

chrn is vector of chromosome number.

*posit* is position vector of *SNP*s on chromosomes. Some time, *chrn* and posit are combined into string *hg19* or *hg18*.

 $pv_j$  is defined as *p*-value,  $pc_j$  and  $pd_j$  as proportions of sample size for SNP j to the maximum sample size in causal variables and in disease, respectively.

We use function mktable to choose SNPs and make a standard beta table for MR and path analyses. For convenience, we first assign lpd.data to lpd and cad.data to cad:

The standard beta table will be created via 15 steps:

Step1: calculate pvj

> pvalue.LDL <- lpd\$P.value.LDL > pvalue.HDL <-lpd\$P.value.HDL > pvalue.TG <- lpd\$P.value.TG > pvalue.TC <- lpd\$P.value.TC > pv <- cbind(pvalue.LDL, pvalue.HDL, pvalue.TG, pvalue.TC) > pvj <- apply(pv, 1, min)</pre>

Step2: retrieve causal variables from data lpd and construct a matrix for beta:

```
> beta.LDL <- lpd$beta.LDL
> beta.HDL <- lpd$beta.HDL
> beta.TG <- lpd$beta.TG
> beta.TC <- lpd$beta.TC
> beta <- cbind(beta.LDL, beta.HDL, beta.TG, beta.TC)</pre>
```

Step3: construct a matrix for allele1:

> a1.LDL <- lpd\$A1.LDL
> a1.HDL <- lpd\$A1.HDL
> a1.TG <- lpd\$A1.TG
> a1.TC <- lpd\$A1.TC
> alle1 <- cbind(a1.LDL, a1.HDL, a1.TG, a1.TC)</pre>

Step4: give sample sizes of causal variables and calculate *pcj* 

```
> N.LDL <- lpd$N.LDL
> N.HDL <- lpd$N.HDL
> N.TG <- lpd$N.HDL
> N.TC <- lpd$N.TG
> ss <- cbind(N.LDL, N.HDL, N.TG, N.TC)
> sm <- apply(ss,1,sum)
> pcj <- round(sm/max(sm), 6)</pre>
```

Step5: Construct matrix for frequency of allele1 in each causal variable in 1000G.EUR

- > freq.LDL<-lpd\$Freq.A1.1000G.EUR.LDL</pre>
- > freq.HDL<-lpd\$Freq.A1.1000G.EUR.HDL</pre>
- > freq.TG<-lpd\$Freq.A1.1000G.EUR.TG</pre>
- > freq.TC<-lpd\$Freq.A1.1000G.EUR.TC</pre>
- > freq<-cbind(freq.LDL, freq.HDL, freq.TG, freq.TC)</pre>

Step6: construct matrix for sd of each causal variable (here sd is not specific to SNP j). The following sd values for LDL, HDL, TG and TC were means of standard deviations of these lipoprotein concentrations in plasma over 63 studies from Willer *et al* [10].

> sd.LDL <- rep(37.42, length(pvj))
> sd.HDL <- rep(14.87, length(pvj))
> sd.TG <- rep(92.73, length(pvj))
> sd.TC <- rep(42.74, length(pvj))
> sd <- cbind(sd.LDL, sd.HDL, sd.TG, sd.TC)</pre>

Step7: SNPID and position are retrieved from lpd data:

```
> hg19 <- lpd$SNP_hg19.HDL
> rsid <- lpd$rsid.HDL</pre>
```

Step8: separate chromosome number and *SNP* position using chrp:

```
> chr<-chrp(hg=hg19)</pre>
```

Step9: get new data:

```
> newdata<-cbind(freq,beta,sd,pvj,ss,pcj)</pre>
```

- > newdata<-cbind(chr,rsid,alle1,as.data.frame(newdata))</pre>
- > dim(newdata)

Step10: retrieve data from cad and calculate pdj and frequency of coronary artery disease *cad*, *freq.case* in case population:

```
> hg18.d <- cad$chr_pos_b36
> SNP.d <- cad$SNP #SNPID
> a1.d<- tolower(cad$reference_allele)
> freq.d <- cad$ref_allele_frequency
> pvalue.d <- cad$pvalue
> beta.d <- cad$log_odds
> N.case <- cad$N_case
> N.ctr <- cad$N_control
> N.d <- N.case+N.ctr
> freq.case <- N.case/N.d</pre>
```

Step11: combine these cad variables into new data sheet using cbind

> newcad <- cbind(freq.d, beta.d, N.case, N.ctr, freq.case)</pre>

```
> newcad <- cbind(hg18.d, SNP.d, a1.d, as.data.frame(newcad))</pre>
```

```
> dim(newcad)
```

Step12: give name vector of causal variables:

> varname <-c("CAD", "LDL", "HDL", "TG", "TC")</pre>

Step13: choose *SNPs* using parameters LG, Pv, Pc and Pd and create **standard beta table** using mktable(cdata, ddata, rt,varname,LG, Pv, Pc,Pd)where

*cdata* is beta data of SNPs regressed on causal variables. Here *cdata*=newdata.

ddata is beta data of SNPs regressed on the disease (here CAD). Here ddata=newcad.

*LG*: a numeric parameter. *LG* is used to choose *SNP*s with given interval threshold for linkage disequilibrium (*LD*). Default LG = 10.

Pv:a numeric parameter. Pv is used to choose SNPs with a given p-value cutoff. Default  $Pv = 5 \times 10^{-8}$ .

Pc: a numeric parameter. Pc is used to choose *SNP*s with a given cutoff for the proportion of sample size to maximum sample size in causal variable data. Default Pc=0.979.

Pd: a numeric parameter. Pd is used to choose SNP with a given cutoff for the proportion of sample size to the maximum sample size in disease data. Default Pd =0.979.

*rt* has two options: "beta" and "path". If rt="beta" or "Beta" or "B", then mktable return a beta coefficient matrix of *SNP*s regressed on causal variables and disease, if rt="path" or "Path" or "P" it returns a path coefficient matrix of *SNP*s directly contributing to causal variables and disease.

> mybeta <- mktable(cdata=newdata, ddata=newcad, rt="beta", varname=varname, LG=1, Pv=0.00000005, Pc=0.979, n
> dim(mybeta)

> beta <- mybeta[,4:8] # standard beta table for path analysis</pre>

> snp <- mybeta[,1:3] # snp data for annotation analysis</pre>

```
> beta<-DataFrame(beta)</pre>
```

> head(beta)

## 4 Two-way Scatter Plots for Beta Values of Disease and Undefined Causal Variables

To roughly display relationship of the undefined causal variables to disease of study, we use simple **R** plot function to create two-way plots of beta of multiple *SNP* regressed on the undefined causal variable versus the disease.

```
> data(beta.data)
```

- > beta.data<-DataFrame(beta.data)</pre>
- > CAD <- beta.data\$cad</pre>
- > LDL <- beta.data\$ldl</pre>
- > HDL <- beta.data\$hdl</pre>
- > TG <- beta.data\$tg</pre>
- > TC <- beta.data\$tc</pre>

> par(mfrow=c(2, 2), mar=c(5.1, 4.1, 4.1, 2.1), oma=c(0, 0, 0, 0))

- > plot(LDL,CAD, pch=19, col="blue", xlab="beta of SNPs on LDL", ylab="beta of SNP on CAD", cex.lab=1.5, cex.d > abline(lm(CAD~LDL), col="red", lwd=2)
- > plot(HDL, CAD, pch=19,col="blue", xlab="beta of SNPs on HDL", ylab="beta of SNP on CAD", cex.lab=1.5, cex.
- > abline(lm(CAD~HDL), col="red", lwd=2)
- > plot(TG, CAD, pch=19, col="blue", xlab="beta of SNPs on TG", ylab="beta of SNP on CAD",cex.lab=1.5, cex.ax.
- > abline(lm(CAD~TG), col="red", lwd=2)
- > plot(TC,CAD, pch=19, col="blue", xlab="beta of SNPs on TC", ylab="beta of SNP on CAD", cex.lab=1.5, cex.ax.
- > abline(lm(CAD~TC), col="red", lwd=2)

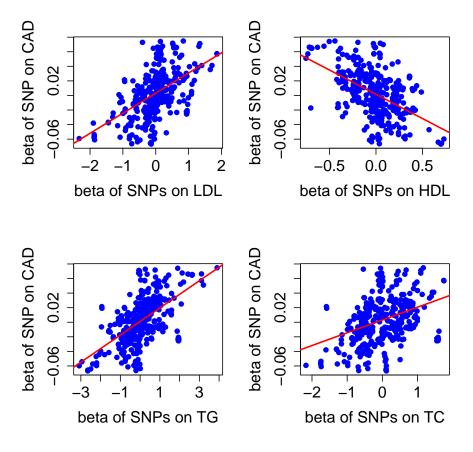


Figure 1: Scatter plots of lipid versus coronary artery disease (CAD) based on beta values of 368 SNPs regression analyses

### 5 MR and Path Analysis

After **standard beta table** was successfully created by **mktable**, user can use function **path** to perform RM analysis (regression analysis of causal variable beta values on the disease or outcome beta values), correlation among the undefined causal variables and disease and path analyses with model of

$$y \sim x_1 + x_2 + \dots + x_m$$

where y is disease or outcome variable,  $x_i$  is undefined causal variable i. Path analysis is based on RM analysis(regression coefficients of the causal beta on the disease beta). path will produce three tables: beta coefficients, sd values and t-test results of causal variables on disease or outcome, correlation matrix and path matrix(direct and indirect path coefficients)

```
> data(beta.data)
```

- > mybeta <- DataFrame(beta.data)</pre>
- > mod <- CAD~LDL+HDL+TG+TC</pre>
- > pathvalue <- path(betav=mybeta, model=mod, outcome="CAD")</pre>

#### 6 Create Path Diagram

Once user finished performance of path, user will have correlation matrix and direct path coefficients of undefined causal variable onto the disease. User is required to open a *csv* file saving results of path analysis and make table in **R Console** or copy correlation matrix without disease correlation coefficients to *excel* and copy direct path coefficients to the last column. Here is an example of making correlation and path table:

```
> mypath <- matrix(NA,3,4)
> mypath[1,] <- c(1.000000, -0.066678, 0.420036, 0.764638)
> mypath[2,] <- c(-0.066678, 1.000000, -0.559718, 0.496831)
> mypath[3,] <- c(0.420036, -0.559718, 1.000000, 0.414346)
> colnames(mypath) <- c("LDL", "HDL", "TG", "path")
> mypath<-as.data.frame(mypath)
> mypath
LDL HDL TG path
1 1.000000 -0.066678 0.420036 0.764638
2 -0.066678 1.000000 -0.559718 0.496831
3 0.420036 -0.559718 1.000000 0.414346
```

The last column is direct path coefficients, we use "path" to name this column. With this table (for example, mypath), user can use functionpathdiagram(pathdata,disease,R2,range) to create path diagram. Here

*pathdata* is path result data consisting of causal correlation matrix and direct path coefficient vectors.

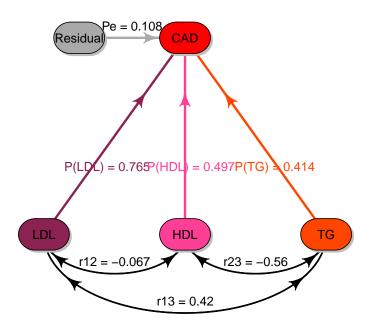
*disease* is a string that specifies disease name. If the disease name is long or has multiple words, then we suggest an abbreviated name, for example, coronary artery disease are shorted as "CAD".

R2, a numeric parameter, is R-square obtained from path analysis.

range is range of specified columns for correlation matrix. For example, range = c(2:4) means the correlation coefficient begins with column 2 and end at column 4. For our current example, range=c(1:3).

```
> library(diagram)
```

> pathdiagram(pathdata=mypath, disease="CAD", R2=0.988243, range=c(1:3))



**Figure 2:** Path diagram demo. This path diagram shows the direct risk effects of causal variables *LDL*, *HDL* and *TG* on the disease *CAD* and their correlations.

### 7 Create Two-level Nested Path Diagram

Consider one of the causal variables is outcome of the other causal variables, but we also concern if all variables are risk factors for the disease of study. In this case we want to construct two-level nested path diagram using function <a href="mailto:pathdiagram2">pathdiagram2</a> (pathD, pathO, rangeD, rangeO, disease, R2D, R2O) where

pathD is a R object that is disease path result data consisting of correlation matrix of undefined causal variables to be identified in Mendelian randomization analysis and path coefficient vector of these variables directly causing the disease of study.

pathO is a R object that is outcome path result data consisting of correlation matrix of undefined causal variables and path coefficient vector of these variables directly contributing to outcome. This outcome variable may be one of risk factors or causal variables in disease path data. These variables in *pathO* are the same with those in *pathD*.

rangeD is numeric vector, specifies column range for correlation coefficient matrix in *pathD*, for example, rangeD=c(2:4) means the correlation coefficient begins with column 2 and end at column 4.

*rangeO* is numeric vector, specifies column range for correlation coefficient matrix in *pathO*, see example in *rangeD*.

*disease* is a string that specifies disease name. If the disease name is long or has multiple words, then we suggest an abbreviated name, for example, *"coronary artery disease"* can be shortened as *"CAD"*.

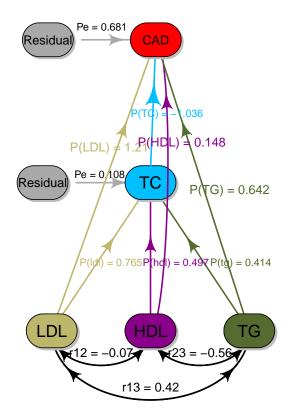
Here is an example of *pathD* data:

```
> pathD<-matrix(NA,4,5)</pre>
> pathD[1,] <- c(1,
                            -0.070161, 0.399038, 0.907127, 1.210474)
> pathD[2,] <- c(-0.070161,</pre>
                                    1, -0.552106, 0.212201, 0.147933)
> pathD[3,] <- c(0.399038, -0.552106, 1, 0.44100, 0.64229)</pre>
> pathD[4,] <- c(0.907127, 0.212201, 0.441007, 1, -1.035677)
> colnames(pathD) <- c("LDL", "HDL", "TG", "TC", "path")</pre>
> pathD<-as.data.frame(pathD)</pre>
> pathD
        LDL
                   HDL
                              ΤG
                                       тс
                                                path
1 1.000000 -0.070161 0.399038 0.907127 1.210474
2 -0.070161 1.000000 -0.552106 0.212201 0.147933
3 0.399038 -0.552106 1.000000 0.441000 0.642290
4 0.907127 0.212201 0.441007 1.000000 -1.035677
```

Using pathD and mypath, we can perform function pathdiagram2 to create a two-level nested path diagram:

> pathdiagram2(pathD=pathD,pathO=mypath,rangeD=c(1:4),rangeO=c(1:3),disease="CAD", R2D=0.536535,R2O=0.988243

Note that in the current version, *GMRP* can just create two-level nested path diagram, maybe in the later version, *GMRP* will create more complex path diagrams such as more than one inner path diagram andor multiple-disease path diagram using structure equations.



**Figure 3:** Demo of two-level nested *pathdiagram*. The outside *pathdiagram* shows the direct risk effects of undefined causal variables *LDL*, *HDL*, *TG* and *TC* on the disease *CAD*, the inner *pathdiagram* indicates the direct contributions of *LDL*, *HDL* and *TG* to *TC* and the correlation relationships among these variables.

### 8 SNP Annotation Analysis

*SNP*s chosen will be annotated in function and chromosome position. Position annotation analysis will give position information of these selected *SNP*s on chromosomes including chromosome distribution and averaged intervals between *SNP*s. We use snpposit to perform *SNP* position annotation. This package provides 358 *SNP*s selected by mktable.

```
> data(SNP358.data)
```

```
> SNP358 <- as.data.frame(SNP358.data)</pre>
```

```
> head(SNP358)
```

 rsid
 chr
 posit

 1
 rs10056022
 5
 74969415

 2
 rs10059560
 5
 156405784

 3
 rs10061689
 5
 74771387

 4
 rs10075465
 5
 74970975

 5
 rs10115928
 9
 107650843

 6
 rs10161126
 12
 110042348

head displays data format required by snpposit. User can create similar table for *SNP* position annotation analysis. To create chromosome position histogram, we need *graphics*:

> library(graphics)

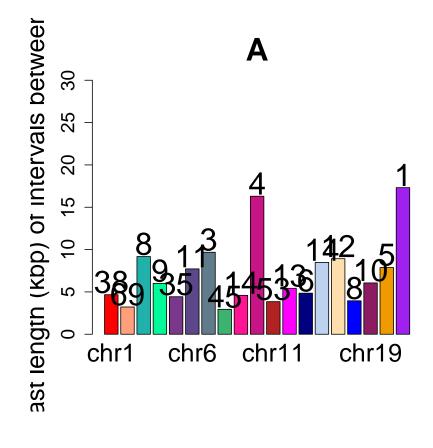
With SNP data SNP358, we can perform *SNP* position annotation using function snpPositAn not (*SNPdata*,*SNPhg19*,*main*) where

*SNPdata* is R object that may be *hg19* that is a string vector(chr##.#########) or two numeric vectors (chromosome number and *SNP* position).

*SNPhg19* is a string parameter. It may be "*hg19*" or "*chr*". If *SNPhg19*="*hg19*",then *SNPdata* contains a string vector of *hg19* or if *SNPhg19*="*chr*", then *SNPdata* consists of at lest two numeric columns: *chr* and *posit*. *chr* is chromosome number and *posit* is *SNP* physical position on chromosomes. Note that "*chr*" and "*posit*" are required column names in *SNPdata* if *SNPhg19*="*chr*".

main is a string which is title of graph. If no title is given, then man="". Its default is "A".

> snpPositAnnot(SNPdata=SNP358,SNP\_hg19="chr",main="A")



**Figure 4:** Chromosomal histogram of 358 selected *SNPs*. Averaged lengths of *SNP* intervals on chromosome mean that the *SNPs* on a chromosome have their averaged lengths of intervals between them. All averaged lengths over 2000kb on chromosomes were truncated, the *SNPs* on these chromosomes have at least 2000kbp length of interval. Numbers above *chr* columns are numbers of *SNP* distributed on the chromosomes

SNP function annotation analysis has two steps:

Step 1: copy *SNP IDs* selected to **Batch Query** box in *SNP* Annotation Tool. After setting parameters and running by clicking *run button*, SNP annotation result will be obtained after running for a while. Choose consequence sheet of *UCSC* and copy the results to excel sheet, "*Predicted function*" column name is changed to "*functionunit*" name and save it as *csv* format.

Step2: input the *csv* file into *R* Console using **R** function read.csv. In *GMRP* package, we have provided data for *SNP* function annotation analysis.

```
> data(SNP368annot.data)
> SNP368<-as.data.frame(SNP368annot.data)</p>
> SNP368[1:10, ]
          SNP Allele Strand
                             Symbol
                                           Gene function_unit
1
  rs10056022
                G|A
                         1
                                POC5 uc003keg.4
                                                  3downstream
2 rs10056022
                 G|A
                         1
                                POC5 uc003keh.4
                                                  3downstream
3 rs10056022
                GIA
                         1 ANKDD1B uc010izt.4
                                                 3downstream
4 rs10056022
                                POC5 uc010izu.3
                G|A
                         1
                                                  3downstream
5
  rs10061689
                GIA
                         1 COL4A3BP uc003kds.3
                                                     intronic
6 rs10061689
                          1 COL4A3BP uc003kdt.3
                G|A
                                                     intronic
7 rs10061689
                          1 COL4A3BP uc003kdu.2
                G|A
                                                     intronic
8 rs10061689
                          1 COL4A3BP uc011csu.2
                G|A
                                                     intronic
9 rs10075465
                C|G
                          1
                                POC5 uc003keg.4
                                                     intronic
10 rs10075465
                          1
                                POC5 uc003keh.4
                 C|G
                                                     intronic
```

We perform function **ucscannot** to summarize proportions of SNPs coming from gene various elements such as code region, introns, etc, and then create 3D pie using **pie3D** of *plotrix*.

> library(plotrix)

 $\ensuremath{\mathsf{ucscannot}}$  has four parameters to be inputted: SNPn, A, B and C, a method and UCSC annotated data:

UCSCannot is annotation data obtained by performing SNP tools.

SNPn is numeric parameter for number of SNPs contained in UCSCannot

A is numeric parameter for title size, default=2.5.

B is numeric parameter for label size, default=1.5.

*C* is numeric parameter for *labelrad* distance,default=1.3.

method is numeric parameter for choosing figure output methods. It has two options: method=1 has no legend but color and pie components are labeled with gene elements, method=2 has legend over pie. The default = 1.

> ucscannot(UCSCannot=SNP368, SNPn=368)

g	enes	exons	introns	TUR3	UTR5	intergenes	upstream	downstream
[1,]	166 0.01	234568	0.8138651	0.01424501	0.001899335	0.004748338	0.05508072	0.09781576

> ucscannot(UCSCannot=SNP368, SNPn=368, A=3, B=2, C=1.3, method=2)

g	enes e	xons in	trons	TUR3	UTR5 int	tergenes ι	upstream dow	wnstream
[1,]	166 0.0123	4568 0.81	38651 0.0142	4501 0.00189	9335 0.00	04748338 0.0	95508072 0.0	99781576

**GWAS-based Mendelian Randomization Path Analysis** 

genes exons introns TUR3 UTR5 intergenes upstream downstream [1,] 166 0.01234568 0.8138651 0.01424501 0.001899335 0.004748338 0.05508072 0.09781576

# :ion of 368 SNPs within 16

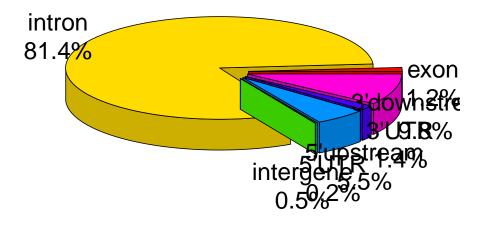
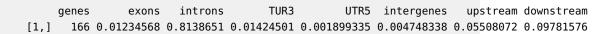


Figure 5: Distribution of the selected SNPs in gene function elements.



## :ion of 368 SNPs within 16

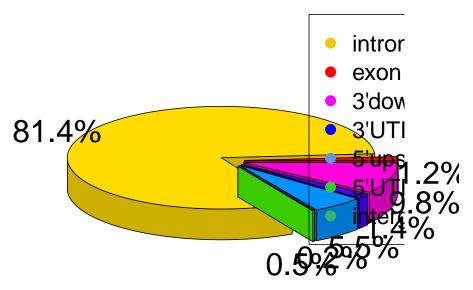


Figure 6: Distribution of the selected SNPs in gene function elements.

#### 9 Session Info

```
> sessionInfo()
R version 4.4.0 RC (2024-04-16 r86468)
Platform: x86_64-pc-linux-gnu
Running under: Ubuntu 22.04.4 LTS
Matrix products: default
BLAS: /home/biocbuild/bbs-3.20-bioc/R/lib/libRblas.so
LAPACK: /usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.10.0
locale:
 [1] LC_CTYPE=en_US.UTF-8
                                LC_NUMERIC=C
                                                            LC_TIME=en_GB
 [4] LC_COLLATE=C
                                LC_MONETARY=en_US.UTF-8
                                                            LC_MESSAGES=en_US.UTF-8
 [7] LC_PAPER=en_US.UTF-8
                                LC_NAME=C
                                                            LC_ADDRESS=C
[10] LC_TELEPHONE=C
                                LC_MEASUREMENT=en_US.UTF-8 LC_IDENTIFICATION=C
time zone: America/New_York
tzcode source: system (glibc)
attached base packages:
[1] stats4
              stats
                        graphics grDevices utils
                                                      datasets methods
                                                                           base
other attached packages:
[1] GMRP_1.33.0
                         GenomicRanges_1.57.0 GenomeInfoDb_1.41.0 IRanges_2.39.0
[5] S4Vectors_0.43.0
                         BiocGenerics_0.51.0 plotrix_3.8-4
                                                                    diagram_1.6.5
[9] shape_1.4.6.1
loaded via a namespace (and not attached):
 [1] httr_1.4.7
                             cli_3.6.2
                                                      knitr_1.46
 [4] rlang_1.1.3
                             xfun_0.43
                                                      UCSC.utils_1.1.0
 [7] jsonlite_1.8.8
                             BiocStyle_2.33.0
                                                      htmltools_0.5.8.1
[10] rmarkdown_2.26
                             evaluate_0.23
                                                      fastmap_1.1.1
[13] yaml_2.3.8
                             BiocManager_1.30.22
                                                      compiler_4.4.0
[16] XVector_0.45.0
                             digest_0.6.35
                                                      R6_2.5.1
[19] GenomeInfoDbData_1.2.12 tools_4.4.0
                                                      zlibbioc_1.51.0
```

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